EE 330 Lecture 24

- Small Signal Models
- Small Signal Analysis

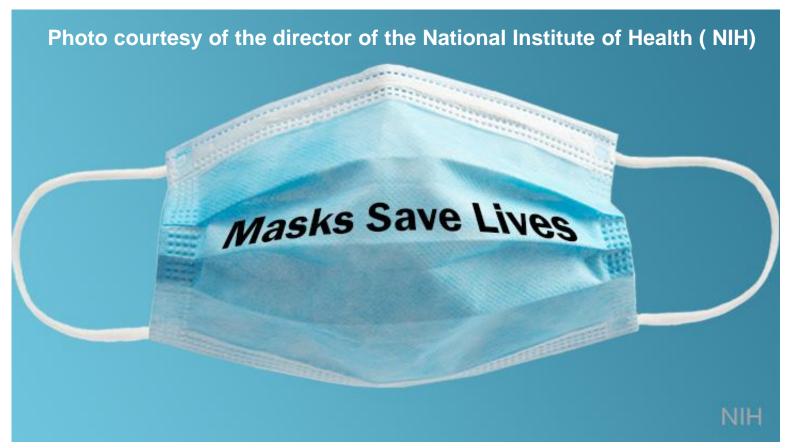
Exam Schedule

Exam 1 Friday Sept 24

Exam 2 Friday Oct 22

Exam 3 Friday Nov 19

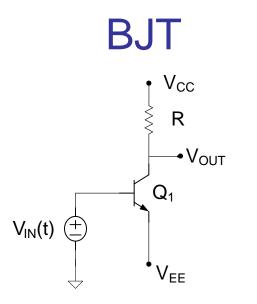
Final Tues Dec 14 12:00 p.m.



As a courtesy to fellow classmates, TAs, and the instructor

Wearing of masks during lectures and in the laboratories for this course would be appreciated irrespective of vaccination status

Comparison of Gains for MOSFET and BJT Circuits



$$\begin{array}{c|c}
 & V_{DD} \\
 & R_1 \\
 & V_{OUT}
\end{array}$$

MOSFET

$$\mathsf{A}_{_{\mathsf{VB}}} = -\frac{\mathsf{I}_{_{\mathsf{CQ}}} \mathsf{R}_{_{\mathtt{1}}}}{\mathsf{V}_{_{\mathtt{t}}}}$$

$$A_{_{\text{VM}}} = \frac{2I_{_{\text{DQ}}}R}{\left[V_{_{\text{SS}}} + V_{_{\text{T}}}\right]}$$

If
$$I_{DQ}R = I_{CQ}R_1 = 2V$$
, $V_{SS} + V_T = -1V$, $V_t = 25mV$

$$A_{VB} = -\frac{I_{CQ}R_{1}}{V_{T}} = -\frac{2V}{25mV} = -80 \qquad A_{VM} = \frac{2I_{DQ}R}{\left[V_{SS} + V_{T}\right]} = \frac{4V}{-1V} = -4$$

$$A_{VM} = \frac{2I_{DQ}R}{[V_{SS} + V_{T}]} = \frac{4V}{-1V} = -4$$

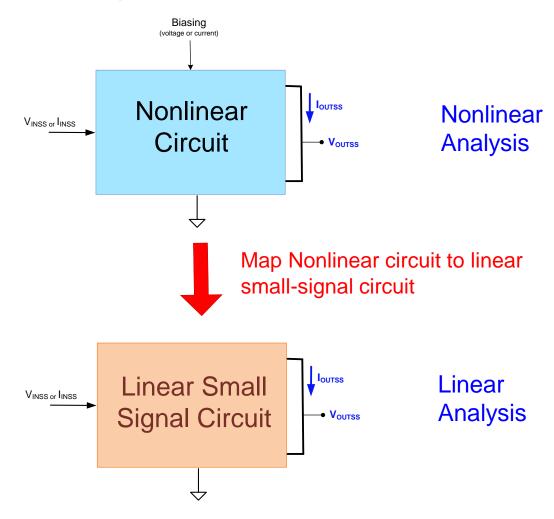
Observe A_{VB}>>A_{VM}

Due to exponential-law rather than square-law model

Operation with Small-Signal Inputs

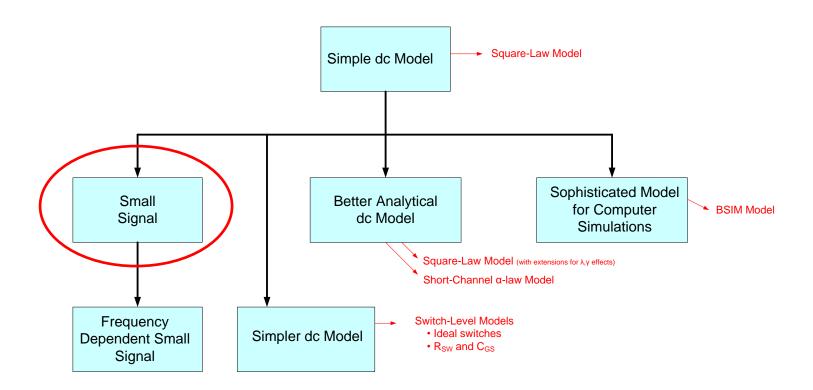
- Analysis procedure for these simple circuits was very tedious
- This approach will be unmanageable for even modestly more complicated circuits
- Faster analysis method is needed!

Small-Signal Analysis



- Will commit next several lectures to developing this approach
- Analysis will be MUCH simpler, faster, and provide significantly more insight
- Applicable to many fields of engineering

Small-Signal Analysis



Operation with Small-Signal Inputs

Why was this analysis so tedious?

Because of the nonlinearity in the device models

What was the key technique in the analysis that was used to obtain a simple expression for the output (and that linearly related the output to the input)?

$$V_{\text{OUT}} = V_{\text{CC}} - J_{\text{S}} A_{\text{E}} R_{1} e^{\frac{V_{beQ}}{V_{\text{t}}}} e^{\frac{V_{\text{M}} \sin(\omega t)}{V_{\text{t}}}}$$

$$V_{\text{OUT}} \cong \left[V_{\text{CC}} - I_{cQ} R_{1} \right] - \left(\frac{I_{cQ} R_{1}}{V_{t}} \right) V_{\text{M}} \sin(\omega t)$$

Linearization of the nonlinear output expression at the operating point

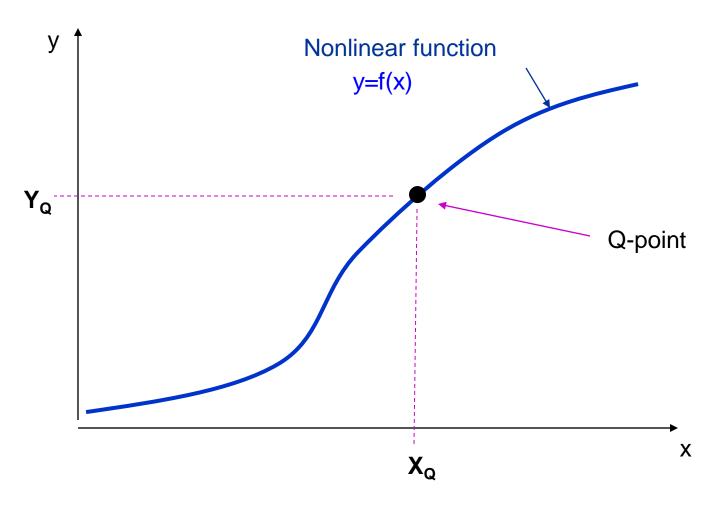
Operation with Small-Signal Inputs

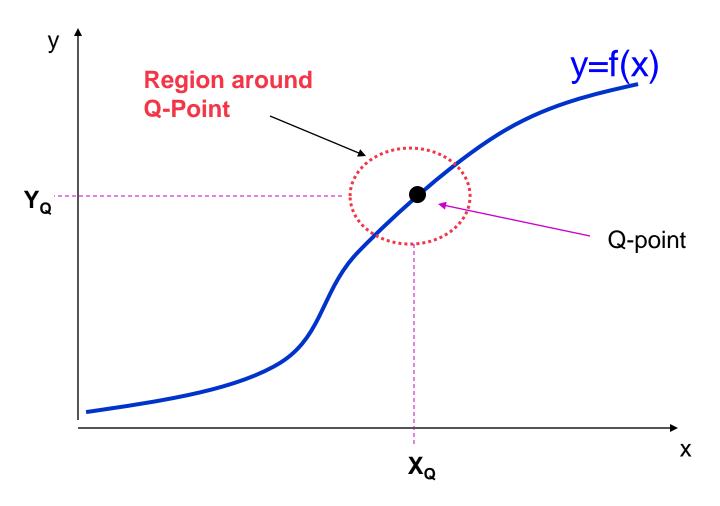
$$\mathbf{I_{CQ}} = \mathbf{J_SA_E}\mathbf{e}^{rac{\mathbf{V_{beQ}}}{\mathbf{V_t}}}$$

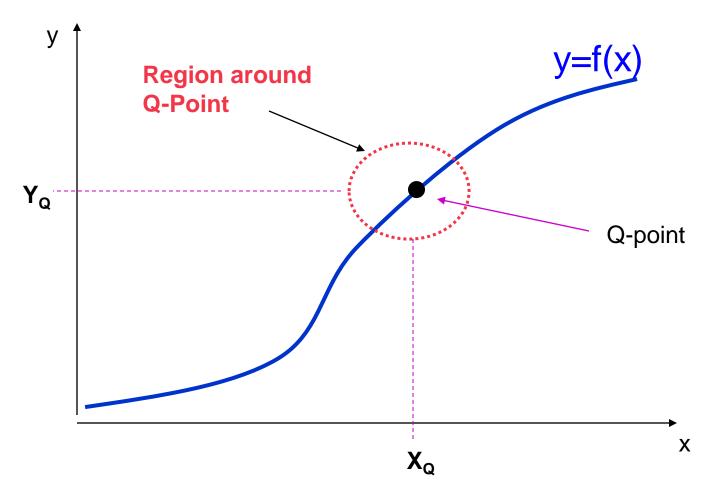
$$V_{\text{OUT}} \cong \begin{bmatrix} V_{\text{cc}} - I_{c\varrho} R_{1} \\ Quiescent \ Output \end{bmatrix} - \underbrace{\begin{pmatrix} I_{\text{cq}} R_{1} \\ V_{t} \end{pmatrix}}_{\text{SS Voltage Gain}} V_{\text{M}} \sin(\omega t)$$

Small-signal analysis strategy

- Obtain Quiescent Output (Q-point)
- 2. Linearize circuit at Q-point instead of linearize the nonlinear solution (this will be done by linearizing each component in the circuit)
- 1. Analyze linear "small-signal" circuit
- 2. Add quiescent and small-signal outputs to obtain good approximation to actual output

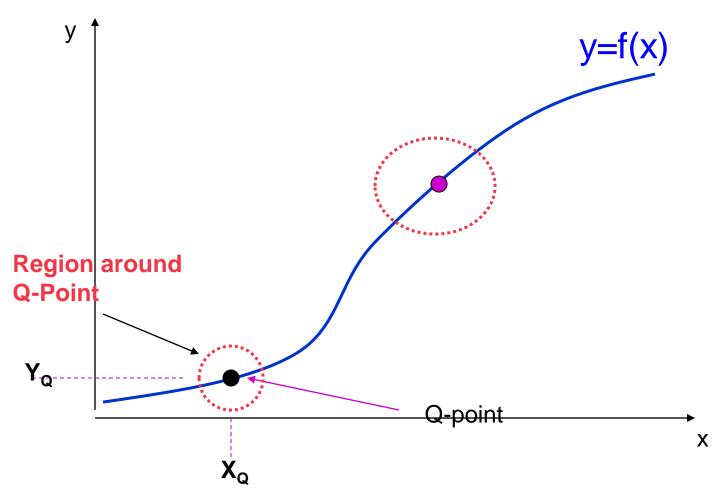






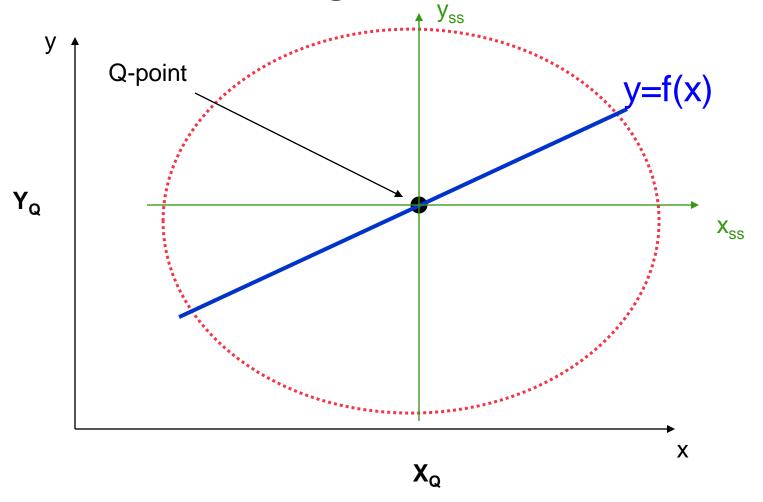
Relationship is nearly linear in a small enough region around Q-point Region of linearity is often quite large

Linear relationship may be different for different Q-points

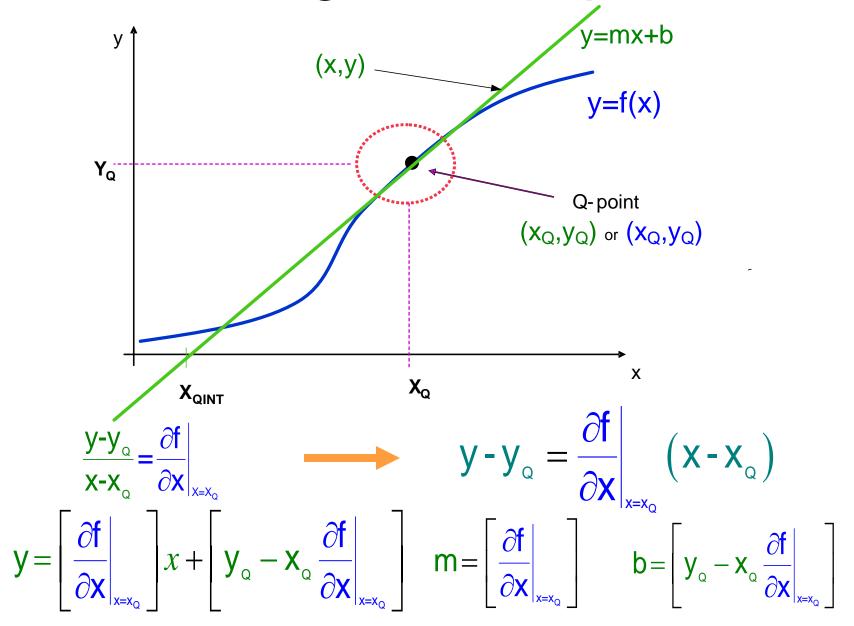


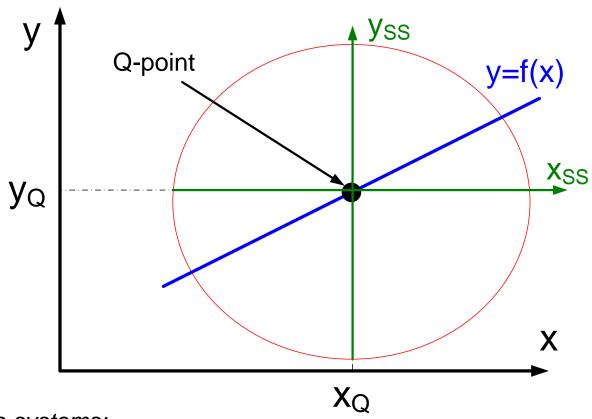
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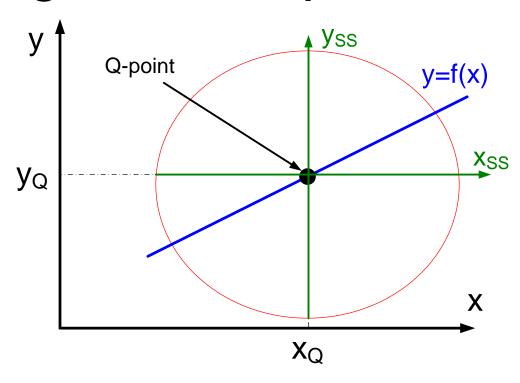
Device Behaves Linearly in Neighborhood of Q-Point Can be characterized in terms of a small-signal coordinate system





Changing coordinate systems:

$$y_{SS} = y - y_{Q} \qquad y - y_{Q} = \frac{\partial f}{\partial x} \bigg|_{x = x_{Q}} \left(x - x_{Q} \right) \longrightarrow y_{SS} = \frac{\partial f}{\partial x} \bigg|_{x = x_{Q}} x_{SS}$$



Small-Signal Model:

$$\mathbf{y}_{ss} = \frac{\partial \mathbf{f}}{\partial \mathbf{x}} \Big|_{\mathbf{x}=\mathbf{x}} \mathbf{x}_{ss}$$

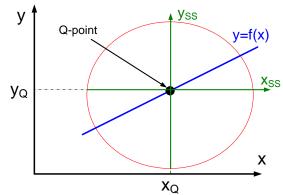
- Linearized model for the nonlinear function y=f(x)
- Valid in the region of the Q-point
- Will show the small signal model is simply Taylor's series expansion of f(x) at the Q-point truncated after first-order terms

Observe:

$$y - y_{Q} = \frac{\partial f}{\partial x}\Big|_{x=x_{Q}} (x - x_{Q}) \longrightarrow y_{SS} = \frac{\partial f}{\partial x}\Big|_{x=x_{Q}} x_{SS}$$

$$y_{Q} = f(x_{Q})$$

$$y = f(x_{Q}) + \frac{\partial f}{\partial x}\Big|_{x=x_{Q}} (x - x_{Q})$$



Recall Taylors Series Expansion of nonlinear function at expansion point x_n

$$y=f(x_0)+\sum_{k=1}^{\infty}\left(\frac{1}{k!}\frac{df}{dx}\Big|_{x=x_0}(x-x_0)^k\right)$$

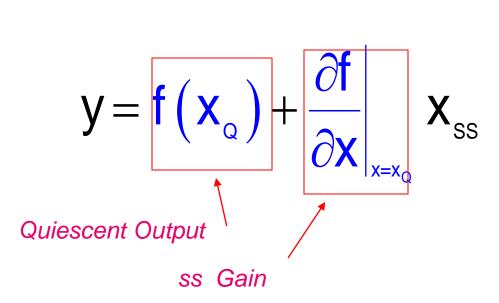
Small-Signal Model:

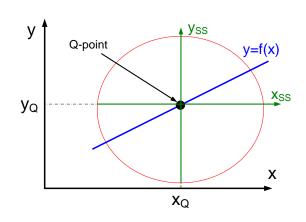
Truncating after first-order terms (and defining "o" as "Q")

$$y \cong f(x_{Q}) + \frac{\partial f}{\partial x}\Big|_{x=x_{Q}} (x-x_{Q}) \qquad y_{SS} = \frac{\partial f}{\partial x}\Big|_{x=x_{Q}} x_{SS}$$

$$\mathbf{y}_{ss} = \frac{\partial \mathbf{f}}{\partial \mathbf{x}} \bigg|_{\mathbf{x} = \mathbf{x}_0} \mathbf{x}_{ss}$$

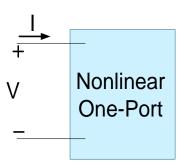
Mathematically, linearized model is simply Taylor's series expansion of the nonlinear function f at the Q-point truncated after first-order terms with notation $x_0 = x_0$



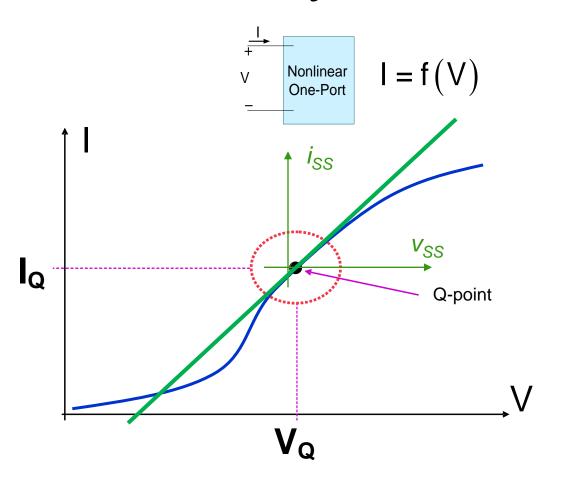


How can a <u>circuit</u> be linearized at an operating point as an alternative to linearizing a nonlinear function at an operating point?

Consider arbitrary nonlinear one-port network



Arbitrary Nonlinear One-Port



Linear model of the nonlinear device at the Q-point

$$i_{SS} = \frac{\partial I}{\partial V} \bigg|_{V = V_{Q}} v_{SS}$$

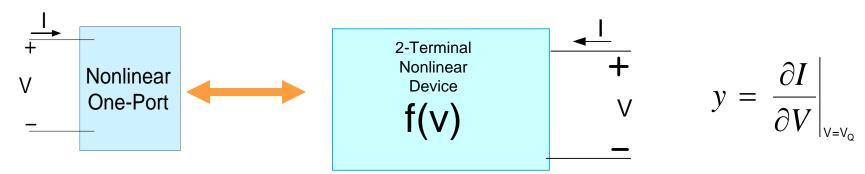
$$i_{SS} = \mathbf{i}$$

$$v_{_{\mathrm{SS}}} = v$$

$$y = \left. rac{\partial I}{\partial V} \right|_{\mathsf{V}=\mathsf{V}_0}$$

$$i = y V$$

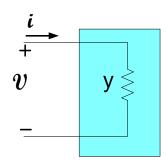
Arbitrary Nonlinear One-Port



Linear small-signal model:

$$i = y v$$

A Small Signal Equivalent Circuit:



- The small-signal model of this 2-terminal electrical network is a resistor of value 1/y
 or a conductor of value y
- One small-signal parameter characterizes this one-port but it is dependent on Qpoint
- This applies to ANY nonlinear one-port that is differentiable at a Q-point (e.g. a diode)

Goal with small signal model is to predict performance of circuit or device in the vicinity of an operating point (Q-point)

Will be extended to functions of two and three variables (e.g. BJTs and MOSFETs)

Solution for the example of the previous lecture was based upon solving the nonlinear circuit for V_{OUT} and then linearizing the solution by doing a Taylor's series expansion

- Solution of nonlinear equations very involved with two or more nonlinear devices
- Taylor's series linearization can get very tedious if multiple nonlinear devices are present

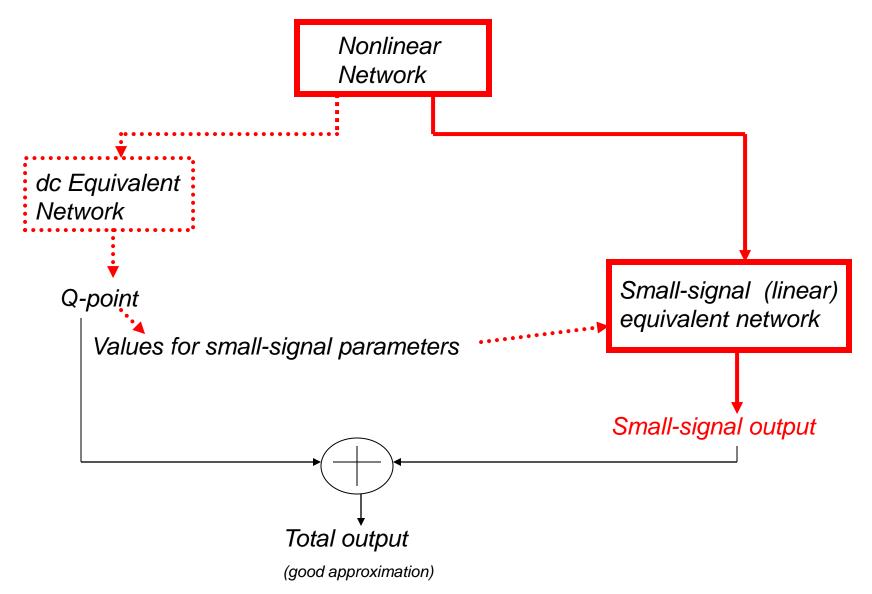
Natural approach to small-signal analysis of nonlinear networks

- 1. Solve nonlinear network
- 2. Linearize solution

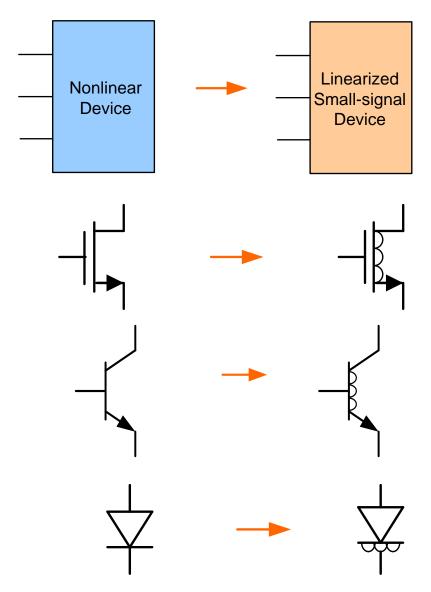
Alternative Approach to small-signal analysis of nonlinear networks

- 1.Linearize nonlinear devices (all)
- 2. Obtain small-signal model from linearized device models
- 3. Replace all devices with small-signal equivalent
- 4 .Solve linear small-signal network

"Alternative" Approach to small-signal analysis of nonlinear networks



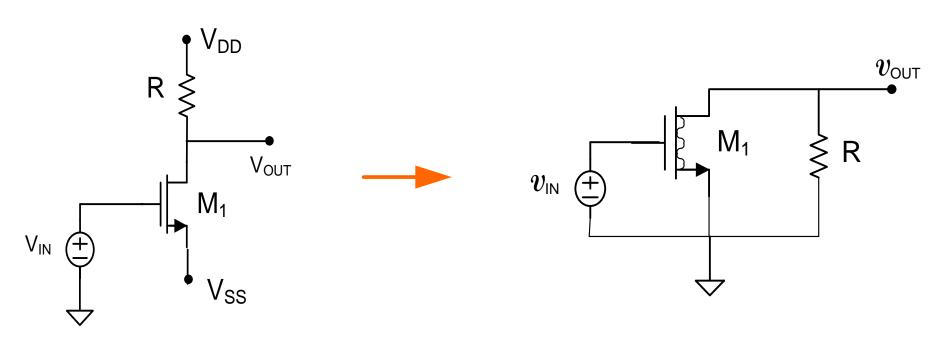
Linearized nonlinear devices



This terminology will be used in THIS course to emphasize difference between nonlinear model and linearized small signal model

Example:

It will be shown that the nonlinear circuit has the linearized small-signal network given

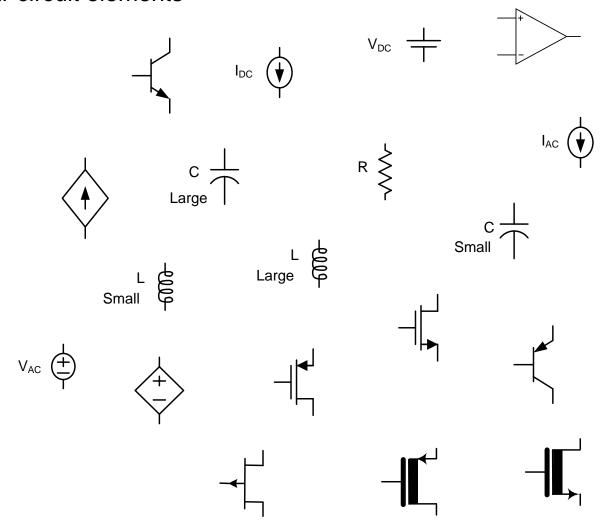


Nonlinear network

Linearized smallsignal network

Linearized Small-Signal Circuit Elements

Must obtain the linearized small-signal circuit element for ALL linear and nonlinear circuit elements

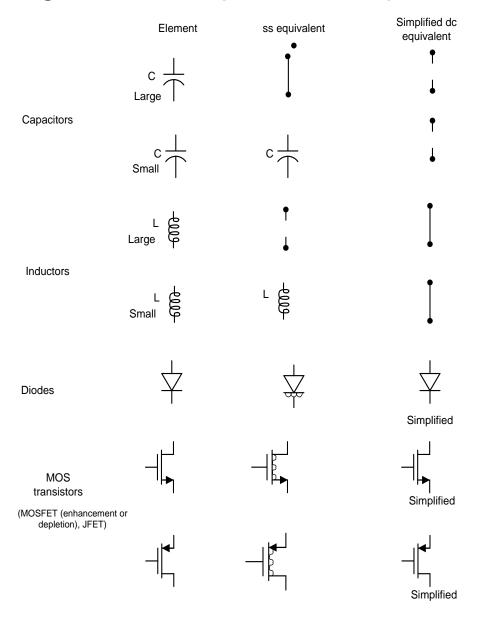


(Will also give models that are usually used for Q-point calculations: Simplified dc models)

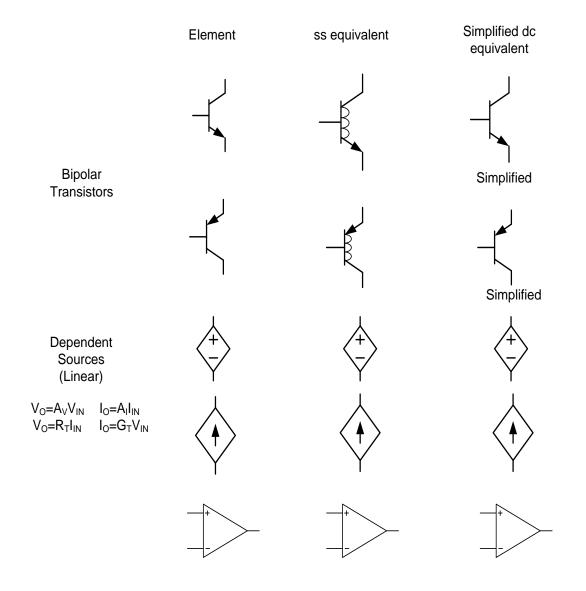
Small-signal and simplified dc equivalent elements

	Element	ss equivalent	Simplified dc equivalent
dc Voltage Source	V _{DC} $\frac{1}{1}$		V _{DC} $\frac{1}{1}$
ac Voltage Source	V _{AC}	V _{AC} $\stackrel{+}{\longleftrightarrow}$	
dc Current Source	I _{DC}	† •	I _{DC}
ac Current Source	I _{AC}	I _{AC}	† •
Resistor	R 奏	R 奏	R

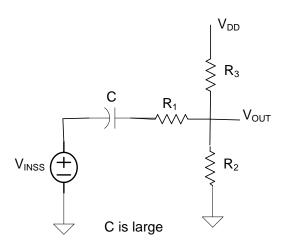
Small-signal and simplified dc equivalent elements

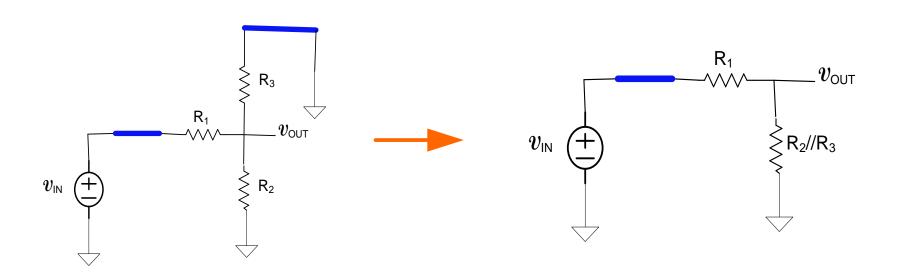


Small-signal and simplified dc equivalent elements

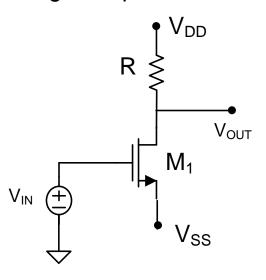


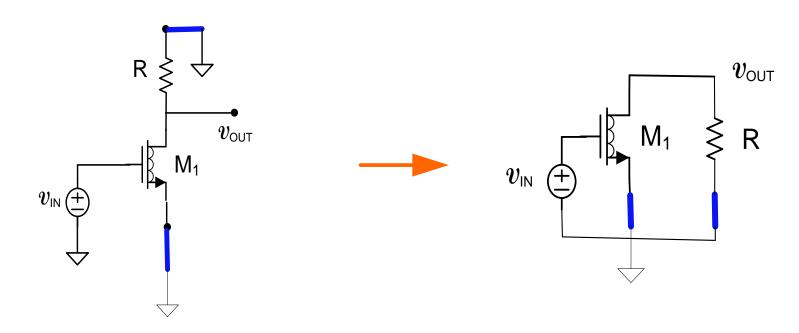
Example: Obtain the small-signal equivalent circuit



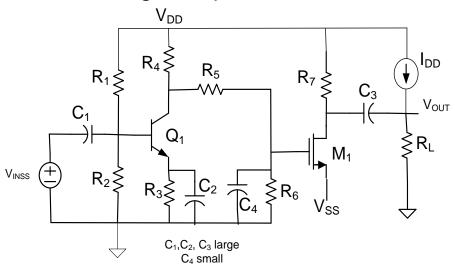


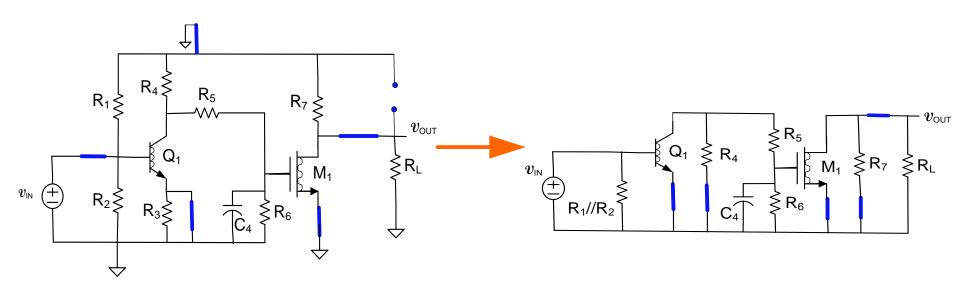
Example: Obtain the small-signal equivalent circuit





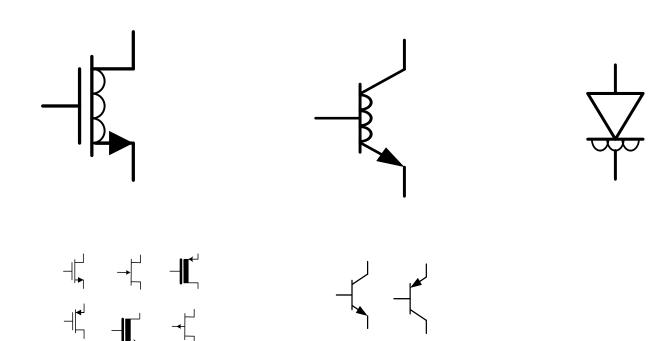
Example: Obtain the small-signal equivalent circuit



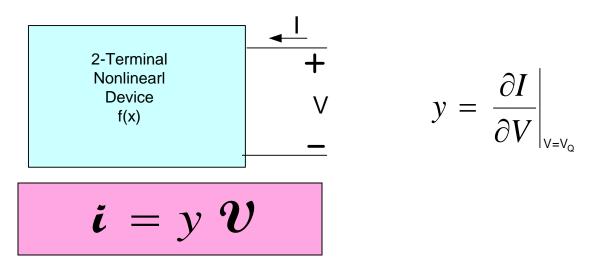


How is the small-signal equivalent circuit obtained from the nonlinear circuit?

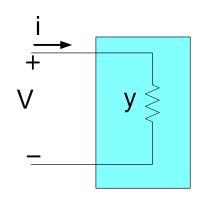
What is the small-signal equivalent of the MOSFET, BJT, and diode?



Small-Signal Diode Model



A Small Signal Equivalent Circuit "Small-signal model"



Thus, for the diode

Small-Signal Diode Model

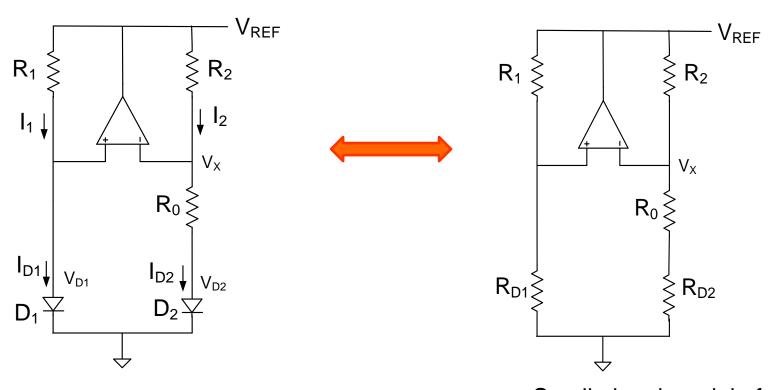
For the diode

$$I_D = I_S e^{V_D/V_t}$$

$$\left. \frac{\partial I_{D}}{\partial V_{D}} \right|_{Q} = \left[\left(I_{S} e^{V_{D}/V_{t}} \right) \frac{1}{V_{t}} \right]_{Q} = \frac{I_{DQ}}{V_{t}}$$

$$R_d = \frac{V_t}{I_{DQ}}$$

Example of diode circuit where small-signal diode model is useful



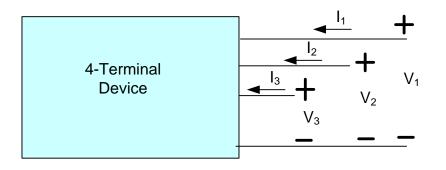
Voltage Reference

Small-signal model of Voltage Reference (useful for compensation when parasitic Cs included)

Small-Signal Model of BJT and MOSFET

Consider 4-terminal network

(3-terminal and 2-terminal and 1-terminal devices then become special cases)



$$I_1 = f_1(V_1, V_2, V_3)$$
 $I_2 = f_2(V_1, V_2, V_3)$
 $I_3 = f_3(V_1, V_2, V_3)$

4 different ways to choose reference terminal

Six port electrical variables {I₁,I₂,I₃,V₁,V₂,V₃}

Number of ways to choose independent variables

$$\binom{6}{3} = \frac{6!}{(6-3)!3!} = 20$$

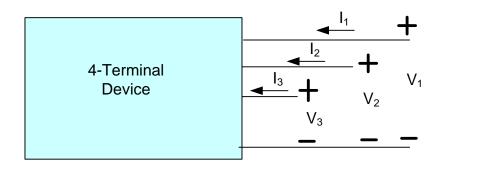
Number of potentially different ways to represent same device

80

We will choose one of these 80 which uses port voltages as independent variables

Small-Signal Model of BJT and MOSFET

Consider 4-terminal network

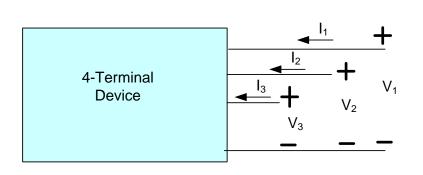


$$egin{aligned} & \mathbf{I_1} = \mathbf{f_1} (\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3}) \ & \mathbf{I_2} = \mathbf{f_2} (\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3}) \ & \mathbf{I_3} = \mathbf{f_3} (\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3}) \end{aligned}$$

Define
$$\begin{aligned} \boldsymbol{i_1} &= \boldsymbol{I_1} - \boldsymbol{I_{1Q}} \\ \boldsymbol{i_2} &= \boldsymbol{I_2} - \boldsymbol{I_{2Q}} \\ \boldsymbol{i_3} &= \boldsymbol{I_3} - \boldsymbol{I_{3Q}} \end{aligned}$$

$$u_1 = V_1 - V_{1Q}$$
 $u_2 = V_2 - V_{2Q}$
 $u_3 = V_3 - V_{3Q}$

Small signal model is that which represents the relationship between the small signal voltages and the small signal currents

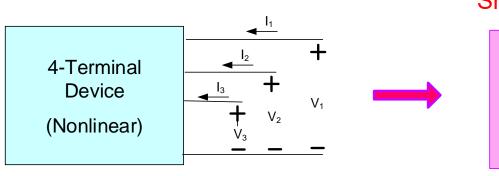


$$i_1 = g_1(v_1, v_2, v_3)$$
 $i_2 = g_2(v_1, v_2, v_3)$
 $i_3 = g_3(v_1, v_2, v_3)$

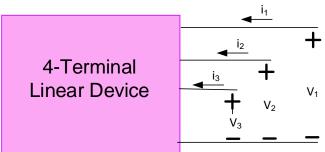
Small signal model is that which represents the relationship between the small signal voltages and the small signal currents

For small signals, this relationship should be linear

Can be thought of as a change in coordinate systems from the large signal coordinate system to the small-signal coordinate system







$$\begin{aligned} & \mathbf{I_1} = \mathbf{f_1} \big(\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3} \big) \\ & \mathbf{I_2} = \mathbf{f_2} \big(\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3} \big) \\ & \mathbf{I_3} = \mathbf{f_3} \big(\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3} \big) \end{aligned}$$

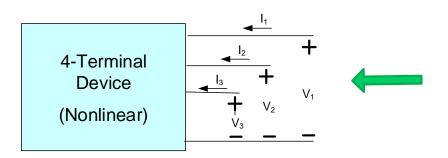
$$\mathbf{i}_1 = g_1(\mathbf{V}_1, \mathbf{V}_2, \mathbf{V}_3)$$

$$\mathbf{i}_2 = g_2(\mathbf{V}_1, \mathbf{V}_2, \mathbf{V}_3)$$

$$\mathbf{i}_3 = g_3(\mathbf{V}_1, \mathbf{V}_2, \mathbf{V}_3)$$

Mapping is unique (with same models)

"Small-signal model"



$$\left. \begin{aligned}
I_{1} &= f_{1}(V_{1}, V_{2}, V_{3}) \\
I_{2} &= f_{2}(V_{1}, V_{2}, V_{3}) \\
I_{3} &= f_{3}(V_{1}, V_{2}, V_{3})
\end{aligned} \right\}$$

$$i_1 = g_1(\boldsymbol{V}_1, \boldsymbol{V}_2, \boldsymbol{V}_3)$$

$$i_2 = g_2(\boldsymbol{V}_1, \boldsymbol{V}_2, \boldsymbol{V}_3)$$

$$i_3 = g_3(\boldsymbol{V}_1, \boldsymbol{V}_2, \boldsymbol{V}_3)$$

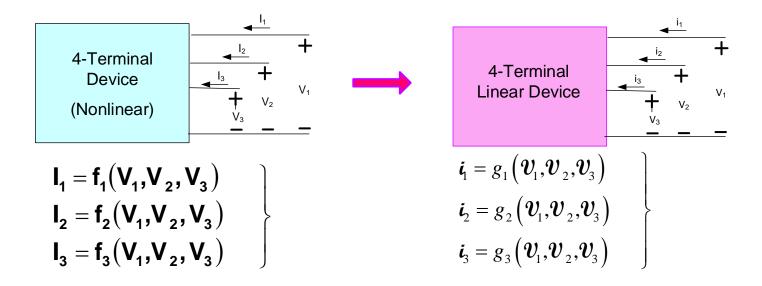
Does inverse mapping exist?

Yes

Is it unique (with same models)?

No

Multiple nonlinear circuits can have same small-signal circuit



Systematic procedure for developing a small-signal model for any nonlinear device will now be developed

Will use 4-terminal device as an example and obtain results for 3-terminal and 2-terminal devices by inspection

Based upon multi-variate Taylor's series expansion truncated after first-order terms

Will then use this procedure to get small-signal model of Diode, MOSFET, BJT, and JFET

Recall for a function of one variable

$$y = f(x)$$

Taylor's Series Expansion about the point x_0 (x_0 is termed the expansion point or the Q-point)

$$y = f(x) = f(x)\Big|_{x=x_0} + \frac{\partial f}{\partial x}\Big|_{x=x_0} (x - x_0) + \frac{\partial^2 f}{\partial x^2}\Big|_{x=x_0} \frac{1}{2!} (x - x_0)^2 + \dots$$

If $x-x_0$ is small

$$y \cong f(x)|_{x=x_0} + \frac{\partial f}{\partial x}|_{x=x_0} (x - x_0)$$

$$y \cong y_0 + \frac{\partial f}{\partial x} \bigg|_{x=x_0} \left(x - x_0 \right)$$

Recall for a function of one variable

$$y = f(x)$$

If $x-x_0$ is small

$$y \cong y_0 + \frac{\partial f}{\partial x} \bigg|_{x=x_0} \left(x - x_0 \right)$$

$$y - y_0 = \frac{\partial f}{\partial x} \bigg|_{x = x_0} \left(x - x_0 \right)$$

If we define the small signal variables as

$$\mathbf{y} = \mathbf{y} - \mathbf{y}_0$$

$$\boldsymbol{x} = \boldsymbol{x} - \boldsymbol{x}_0$$

Recall for a function of one variable

$$y = f(x)$$

If $x-x_0$ is small

$$y \cong y_0 + \frac{\partial f}{\partial x} \bigg|_{x=x_0} \left(x - x_0 \right)$$

$$y - y_0 = \frac{\partial f}{\partial x} \bigg|_{x = x_0} \left(x - x_0 \right)$$

If we define the small signal variables as

$$y = y - y_0$$

$$\boldsymbol{x} = \boldsymbol{x} - \boldsymbol{x}_0$$

Then

$$y = \frac{\partial f}{\partial x}\Big|_{\mathbf{x} = \mathbf{x}} \bullet \mathbf{x}$$

 $y = \frac{\partial f}{\partial x}\Big|_{x = x} \bullet x$ This relationship is linear!

Consider now a function of n variables

$$y = f(x_1,...x_n) = f(\bar{x})$$

If we consider an arbitrary expansion point $\vec{X}_0 = \{x_{10}, x_{20}, ..., x_{n0}\}$

The multivariate Taylor's series expansion around the point $\, ar{X}_{0} \,$ is given by

$$y = f(\vec{x}) = f(\mathbf{x})\Big|_{\vec{x} = \vec{x}_0} + \sum_{k=1}^{n} \left(\frac{\partial f}{\partial \mathbf{x}_k} \Big|_{\vec{x} = \vec{x}_0} (\mathbf{x}_k - \mathbf{x}_{k0}) \right)$$

$$+ \sum_{\substack{k=1 \ j=1}}^{n,n} \left. \frac{\partial^2 f}{\partial \mathbf{x}_j \partial \mathbf{x}_k} \right|_{\vec{x} = \vec{x}_0} \frac{1}{2!} (\mathbf{x}_j - \mathbf{x}_{j0}) (\mathbf{x}_k - \mathbf{x}_{k0}) + ...(H.O.T.)$$

Truncating after first-order terms, we obtain the approximation

$$y - y_0 \cong \sum_{k=1}^n \left(\frac{\partial f}{\partial \mathbf{x}_k} \bigg|_{\bar{x} = \bar{x}_0} \left(\mathbf{x}_k - \mathbf{x}_{k0} \right) \right)$$

where $y_0 = f(\mathbf{x})|_{\vec{x} = \vec{x}_0}$

Multivariate Taylors Series Expansion

$$y = f(x_1,...x_n) = f(\vec{x})$$

Linearized approximation

$$\mathbf{y} - \mathbf{y}_0 \cong \sum_{k=1}^n \left(\frac{\partial f}{\partial \mathbf{x}_k} \bigg|_{\vec{x} = \vec{x}_0} \left(\mathbf{x}_k - \mathbf{x}_{k0} \right) \right)$$

This can be expressed as

$$y_{ss} \cong \sum_{k=1}^{n} a_k x_{ss_k}$$

where

$$\mathbf{y}_{ss} = \mathbf{y} - \mathbf{y}_{0}$$

$$\mathbf{x}_{ss_{k}} = \mathbf{x}_{k} - \mathbf{x}_{k0}$$

$$\mathbf{a}_{k} = \frac{\partial f}{\partial \mathbf{x}_{k}} \Big|_{\mathbf{x} = \mathbf{x}_{k}}$$

Alternate Notation:

$$\boldsymbol{y} \cong \sum_{k=1}^n \mathbf{a}_k \boldsymbol{x}_k$$

$$y = y - y_0$$

$$x_k = X_k - X_{k0}$$

In the more general form¹, the multivariate Taylor's series expansion can be expressed as

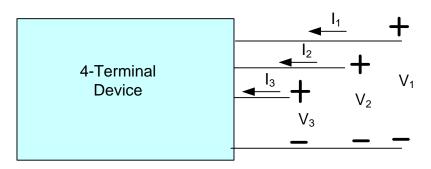
$$f(x_{1},...,x_{n}) = \boldsymbol{\alpha}_{o} + \sum_{m=1}^{\infty} \left(\sum_{\substack{k_{1},\dots,k_{n} \\ j}} \boldsymbol{\alpha}_{k_{1},\dots,k_{n},m} (x_{1} - x_{1,o})^{k_{1}} \cdots (x_{n} - x_{n,o})^{k_{n}} \right)$$
(7)

$$\boldsymbol{\alpha}_{o} = f(x_{1o}, \dots, x_{no})$$

$$\boldsymbol{\alpha}_{k_{1}, \dots, k_{n}; m} = \frac{1}{k_{1}! \cdots k_{n}!} \frac{\boldsymbol{\partial}^{m} f}{\boldsymbol{\partial}^{k_{1}} x_{1} \cdots \boldsymbol{\partial}^{k_{n}} x_{n}} \bigg|_{x_{1o}, \dots, x_{no}}$$
(8)

¹ http://www.chem.mtu.edu/~tbco/cm416/taylor.html

Consider 4-terminal network



$$egin{aligned} & I_1 = f_1(V_1, V_2, V_3) \ & I_2 = f_2(V_1, V_2, V_3) \ & I_3 = f_3(V_1, V_2, V_3) \end{aligned}$$

Nonlinear network characterized by 3 functions each functions of 3 variables

Consider now 3 functions each functions of 3 variables

$$egin{aligned} & I_1 = f_1(V_1, V_2, V_3) \ & I_2 = f_2(V_1, V_2, V_3) \ & I_3 = f_3(V_1, V_2, V_3) \end{aligned}$$

Define

$$\vec{V}_{Q} = \begin{bmatrix} V_{1Q} \\ V_{2Q} \\ V_{3Q} \end{bmatrix}$$

In what follows, we will use $\overline{V}_{\rm Q}$ as an expansion point in a Taylor's series expansion.

Consider now 3 functions each functions of 3 variables

$$\begin{vmatrix}
\mathbf{I}_1 = \mathbf{f_1}(\mathbf{V_1, V_2, V_3}) \\
\mathbf{I_2} = \mathbf{f_2}(\mathbf{V_1, V_2, V_3}) \\
\mathbf{I_3} = \mathbf{f_3}(\mathbf{V_1, V_2, V_3})
\end{vmatrix}$$
Define
$$\vec{V_Q} = \begin{bmatrix} V_{1Q} \\ V_{2Q} \\ V_{3Q} \end{bmatrix}$$

Consider first the function I₁

The multivariate Taylors Series expansion of I_1 , around the operating point \overline{V}_Q . when truncated after first-order terms, can be expressed as:

$$\begin{split} I_1 &= f_1 \big(\boldsymbol{V}_1, \boldsymbol{V}_2, \boldsymbol{V}_3 \big) \cong f_1 \big(\boldsymbol{V}_{1Q}, \boldsymbol{V}_{2Q}, \boldsymbol{V}_{3Q} \big) + \\ & \frac{\partial f_1 \big(\boldsymbol{V}_1, \boldsymbol{V}_2, \boldsymbol{V}_3 \big)}{\partial \boldsymbol{V}_1} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \big(\boldsymbol{V}_1 - \boldsymbol{V}_{1Q} \big) + \frac{\partial f_1 \big(\boldsymbol{V}_1, \boldsymbol{V}_2, \boldsymbol{V}_3 \big)}{\partial \boldsymbol{V}_2} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \big(\boldsymbol{V}_2 - \boldsymbol{V}_{2Q} \big) + \frac{\partial f_1 \big(\boldsymbol{V}_1, \boldsymbol{V}_2, \boldsymbol{V}_3 \big)}{\partial \boldsymbol{V}_3} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \big(\boldsymbol{V}_3 - \boldsymbol{V}_{3Q} \big) \end{split}$$

or equivalently as:

$$I_1 - I_{1Q} = -\frac{\partial f_1 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_1}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\right) + \frac{\partial f_1 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_2}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_2} - \boldsymbol{V_{2Q}}\right) + \frac{\partial f_1 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_2 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_2 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_3}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_3}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_3}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_3}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_3}, \boldsymbol{V_3}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) + \frac{\partial f_3 \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_Q} \left(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\right) \Bigg|_{\bar{\boldsymbol{V}} =$$

repeating from previous slide:

$$\boldsymbol{I_1} - \boldsymbol{I_{1Q}} = -\frac{\partial f_1 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_1}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\Big) + \frac{\partial f_1 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_2}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_2} - \boldsymbol{V_{2Q}}\Big) + \frac{\partial f_1 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\Big) + \frac{\partial f_2 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\Big) + \frac{\partial f_2 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\Big) + \frac{\partial f_2 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\Big) + \frac{\partial f_2 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\Big) + \frac{\partial f_3 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\Big) + \frac{\partial f_3 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_3} - \boldsymbol{V_{3Q}}\Big) + \frac{\partial f_3 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_3}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1}, \boldsymbol{V_2}, \boldsymbol{V_3}\big)}{\partial \boldsymbol{V_1}} \Bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big)}{\partial \boldsymbol{V_1}} \Big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_{1Q}}\big)}{\partial \boldsymbol{V_1}} \Big(\boldsymbol{V_1} - \boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_{\boldsymbol{Q}}} \Big(\boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_1} \Big(\boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_1} \Big(\boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_1} \Big(\boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_2} \Big(\boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_1} \Big(\boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_1} \Big(\boldsymbol{V_1} - \boldsymbol{V_1}\big) + \frac{\partial f_3 \big(\boldsymbol{V_1} - \boldsymbol{V_1}\big)}{\partial \boldsymbol{V}_$$

Make the following definitions

$$\mathbf{y}_{11} = \frac{\partial \mathbf{f}_{1}(\mathbf{V}_{1}, \mathbf{V}_{2}, \mathbf{V}_{3})}{\partial \mathbf{V}_{1}} \Big|_{\bar{\mathbf{V}} = \bar{\mathbf{V}}_{Q}} \qquad \mathbf{i}_{1} = \mathbf{I}_{1} - \mathbf{I}_{1Q}$$

$$\mathbf{y}_{12} = \frac{\partial \mathbf{f}_{1}(\mathbf{V}_{1}, \mathbf{V}_{2}, \mathbf{V}_{3})}{\partial \mathbf{V}_{2}} \Big|_{\bar{\mathbf{V}} = \bar{\mathbf{V}}_{Q}} \qquad \mathbf{i}_{3} = \mathbf{I}_{3} - \mathbf{I}_{3Q}$$

$$\mathbf{y}_{13} = \frac{\partial \mathbf{f}_{1}(\mathbf{V}_{1}, \mathbf{V}_{2}, \mathbf{V}_{3})}{\partial \mathbf{V}_{3}} \Big|_{\bar{\mathbf{V}} = \bar{\mathbf{V}}_{Q}} \qquad \mathbf{u}_{2} = \mathbf{V}_{2} - \mathbf{V}_{2Q}$$

$$\mathbf{v}_{2} = \mathbf{V}_{3} - \mathbf{V}_{3Q}$$

It thus follows that

$$\mathbf{i}_1 = y_{11}\mathbf{u}_1 + y_{12}\mathbf{u}_2 + y_{13}\mathbf{u}_3$$

This is a linear relationship between the small signal electrical variables!

Small Signal Model Development

Nonlinear Model

Linear Model at \bar{V}_Q (alt. small signal model)

$$I_{1} = f_{1}(V_{1}, V_{2}, V_{3}) \rightarrow i_{1} = y_{11}u_{1} + y_{12}u_{2} + y_{13}u_{3}$$

$$I_{2} = f_{2}(V_{1}, V_{2}, V_{3})$$

$$I_{3} = f_{3}(V_{1}, V_{2}, V_{3})$$

Extending this approach to the two nonlinear functions I₂ and I₃

$$\mathbf{i}_{2} = y_{21}\mathbf{u}_{1} + y_{22}\mathbf{u}_{2} + y_{23}\mathbf{u}_{3}$$
 $\mathbf{i}_{3} = y_{31}\mathbf{u}_{1} + y_{32}\mathbf{u}_{2} + y_{33}\mathbf{u}_{3}$

where

$$\mathbf{y}_{ij} = \frac{\partial \mathbf{f}_{i}(\mathbf{V}_{1}, \mathbf{V}_{2}, \mathbf{V}_{3})}{\partial \mathbf{V}_{j}} \Big|_{\bar{\mathbf{V}} = \bar{\mathbf{V}}_{0}}$$

Small Signal Model Development

Nonlinear Model

Linear Model at \bar{V}_o

(alt. small signal model)
$$I_{1} = f_{1}(V_{1}, V_{2}, V_{3}) \rightarrow i_{1} = y_{11}u_{1} + y_{12}u_{2} + y_{13}u_{3}$$

$$I_{2} = f_{2}(V_{1}, V_{2}, V_{3}) \rightarrow i_{2} = y_{21}u_{1} + y_{22}u_{2} + y_{23}u_{3}$$

$$I_{3} = f_{3}(V_{1}, V_{2}, V_{3}) \rightarrow i_{3} = y_{31}u_{1} + y_{32}u_{2} + y_{33}u_{3}$$

where

$$\mathbf{y_{ij}} = \frac{\partial \mathbf{f_i}(\mathbf{V_1, V_2, V_3})}{\partial \mathbf{V_j}} \bigg|_{\mathbf{V} = \mathbf{V_Q}}$$

$$\mathbf{i}_{1} = y_{11}\mathbf{u}_{1} + y_{12}\mathbf{u}_{2} + y_{13}\mathbf{u}_{3}$$

$$\mathbf{i}_{2} = y_{21}\mathbf{u}_{1} + y_{22}\mathbf{u}_{2} + y_{23}\mathbf{u}_{3}$$

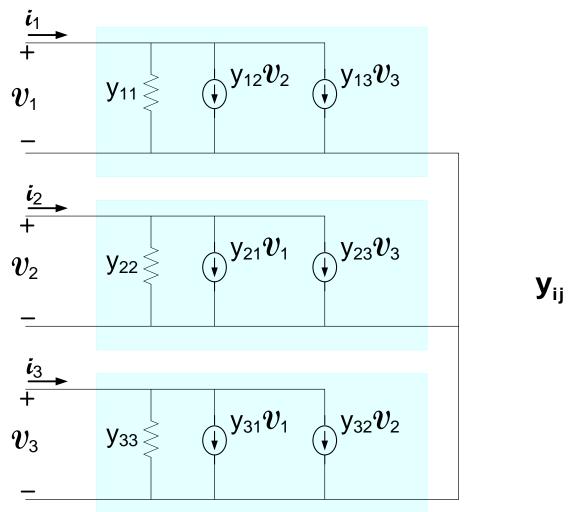
$$\mathbf{i}_{3} = y_{31}\mathbf{u}_{1} + y_{32}\mathbf{u}_{2} + y_{33}\mathbf{u}_{3}$$

where

$$\mathbf{y_{ij}} = \frac{\partial \mathbf{f_i(V_1, V_2, V_3)}}{\partial \mathbf{V_j}} \bigg|_{\vec{\mathbf{V}} = \vec{\mathbf{V}}_{\mathbf{Q}}}$$

- This is a small-signal model of a 4-terminal network and it is linear
- 9 small-signal parameters characterize the linear 4-terminal network
- Small-signal model parameters dependent upon Q-point!
- Termed the y-parameter model or "admittance" –parameter model

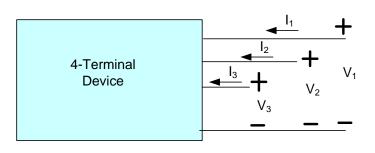
A small-signal equivalent circuit of a 4-terminal nonlinear network (equivalent circuit because has exactly the same port equations)



$$\mathbf{y}_{ij} = \frac{\partial \mathbf{f}_{i}(\mathbf{V}_{1}, \mathbf{V}_{2}, \mathbf{V}_{3})}{\partial \mathbf{V}_{j}}\Big|_{\bar{\mathbf{V}} = \bar{\mathbf{V}}_{\mathbf{Q}}}$$

Equivalent circuit is not unique Equivalent circuit is a three-port network

4-terminal small-signal network summary

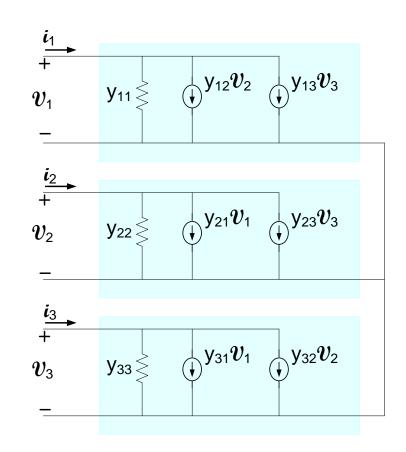


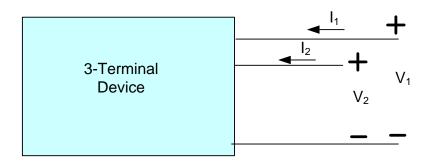
$egin{aligned} & \mathbf{I_1} = \mathbf{f_1} (\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3}) \ & \mathbf{I_2} = \mathbf{f_2} (\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3}) \ & \mathbf{I_3} = \mathbf{f_3} (\mathbf{V_1}, \mathbf{V_2}, \mathbf{V_3}) \end{aligned}$

Small signal model:

$$i1 = y11u1 + y12u2 + y13u3
i2 = y21u1 + y22u2 + y23u3
i3 = y31u1 + y32u2 + y33u3$$

$$\mathbf{y_{ij}} = \frac{\partial f_i(V_1, V_2, V_3)}{\partial V_j} \bigg|_{\vec{V} = \vec{V}_Q}$$





$$\begin{vmatrix}
\mathbf{I_1} = \mathbf{f_1}(\mathbf{V_1, V_2}) \\
\mathbf{I_2} = \mathbf{f_2}(\mathbf{V_1, V_2})
\end{vmatrix}$$

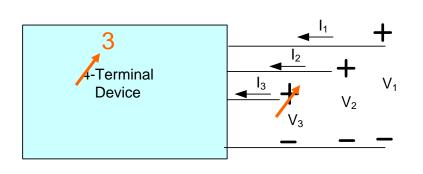
$$\mathbf{i}_{1} = \mathbf{I}_{1} - \mathbf{I}_{1Q}$$

$$\mathbf{i}_{2} = \mathbf{I}_{2} - \mathbf{I}_{2Q}$$

$$u_1 = V_1 - V_{1Q}$$

$$u_2 = V_2 - V_{2Q}$$

Small signal model is that which represents the relationship between the small signal voltages and the small signal currents



$$egin{aligned} \dot{u}_1 &= g_1 ig(v_1, v_2, v_3 ig) \\ \dot{v}_2 &= g_2 ig(v_1, v_2, v_3 ig) \\ \dot{v}_3 &= g_3 ig(v_1, v_2, v_3 ig) \end{aligned}$$

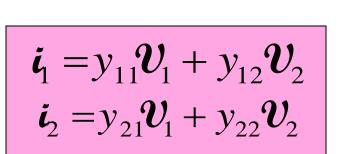
$$\mathbf{i}_{1} = y_{11}\mathbf{v}_{1} + y_{12}\mathbf{v}_{2} + y_{13}\mathbf{v}_{3}$$

$$\mathbf{i}_{2} = y_{21}\mathbf{v}_{1} + y_{22}\mathbf{v}_{2} + y_{23}\mathbf{v}_{3}$$

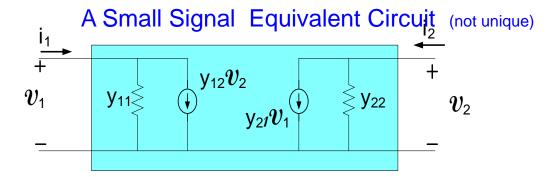
$$\mathbf{i}_{3} = y_{31}\mathbf{v}_{1} + y_{32}\mathbf{v}_{2} + y_{33}\mathbf{v}_{3}$$

$$\mathbf{y}_{ij} = \frac{\partial \mathbf{f}_{i}(\mathbf{V}_{1}, \mathbf{V}_{2}, \mathbf{V}_{3})}{\partial \mathbf{V}_{j}}\bigg|_{\mathbf{V} = \mathbf{V}_{C}}$$

3-Terminal Device

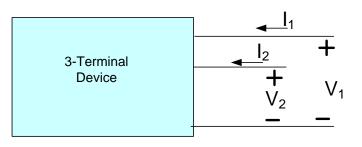


$$\mathbf{y_{ij}} = \frac{\frac{\nabla_2}{-} - \mathbf{v_1}}{\frac{\partial \mathbf{f_i}(\mathbf{V_1, V_2})}{\partial \mathbf{V_j}}} \bigg|_{\mathbf{\bar{V}} = \mathbf{\bar{V}_Q}}$$



- Small-signal model is a "two-port"
- 4 small-signal parameters characterize this 3-terminal linear network
- Small signal parameters dependent upon Q-point

3-terminal small-signal network summary



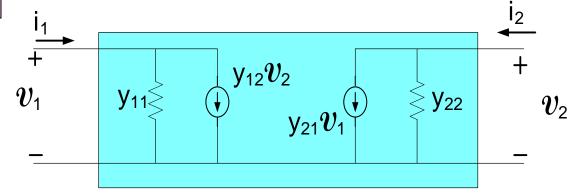
$$I_1 = f_1(V_1, V_2)$$

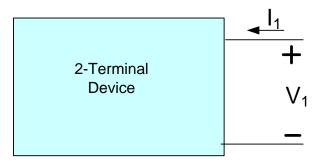
$$I_2 = f_2(V_1, V_2)$$

Small signal model:

$$\mathbf{i}_1 = y_{11} \mathbf{v}_1 + y_{12} \mathbf{v}_2$$
 $\mathbf{i}_2 = y_{21} \mathbf{v}_1 + y_{22} \mathbf{v}_2$

$$\boldsymbol{y}_{ij} = \frac{\partial f_i(\boldsymbol{V_1, V_2})}{\partial \boldsymbol{V_j}} \bigg|_{\bar{\boldsymbol{V}} = \bar{\boldsymbol{V}}_{\boldsymbol{Q}}}$$





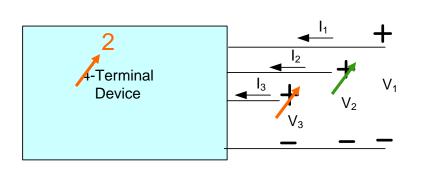
$$I_{\scriptscriptstyle 1}=f_{\scriptscriptstyle 1}(V_{\scriptscriptstyle 1})$$

Define

$$\mathbf{i}_{1} = \mathbf{I}_{1} - \mathbf{I}_{1Q}$$

$$\mathbf{v}_{1} = \mathbf{V}_{1} - \mathbf{V}_{1Q}$$

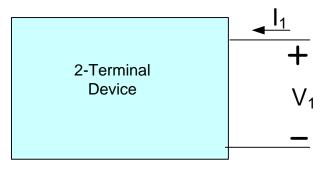
Small signal model is that which represents the relationship between the small signal voltages and the small signal currents



$$egin{aligned} \dot{u}_1 &= g_1 ig(v_1, v_2, v_3 ig) \ \dot{v}_2 &= g_2 ig(v_1, v_2, v_3 ig) \ \dot{v}_3 &= g_3 ig(v_1, v_2, v_3 ig) \end{aligned}$$

$$\mathbf{i}_{1} = y_{11}\mathbf{v}_{1} + y_{12}\mathbf{v}_{2} + y_{13}\mathbf{v}_{3}$$
 $\mathbf{i}_{2} = y_{21}\mathbf{v}_{1} + y_{22}\mathbf{v}_{2} + y_{23}\mathbf{v}_{3}$
 $\mathbf{i}_{3} = y_{31}\mathbf{v}_{1} + y_{32}\mathbf{v}_{2} + y_{33}\mathbf{v}_{3}$

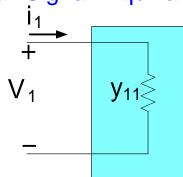
$$\mathbf{y_{ij}} = \frac{\partial f_i(V_1, V_2, V_3)}{\partial V_j}\bigg|_{\bar{V} = \bar{V}_Q}$$



$$\boldsymbol{i}_{1} = y_{11} \boldsymbol{v}_{1}$$

$$\mathbf{y}_{11} = \frac{\partial \mathbf{f}_{1}(\mathbf{V}_{1})}{\partial \mathbf{V}_{1}} \bigg|_{\mathbf{V} = \mathbf{V}_{0}} \qquad \mathbf{V} = \mathbf{V}_{1Q}$$

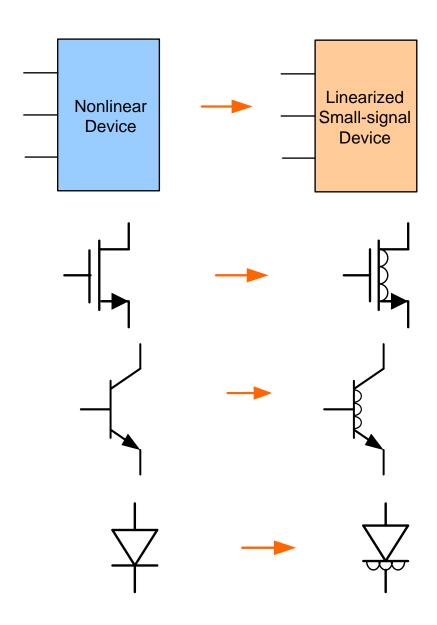
A Small Signal Equivalent Circuit



Small-signal model is a one-port

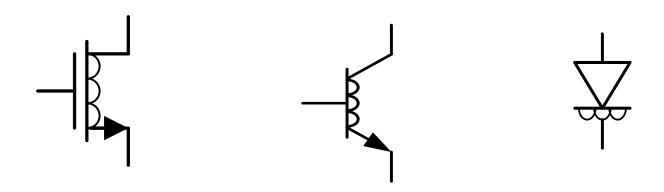
This was actually developed earlier!

Linearized nonlinear devices



How is the small-signal equivalent circuit obtained from the nonlinear circuit?

What is the small-signal equivalent of the MOSFET, BJT, and diode?





Stay Safe and Stay Healthy!

End of Lecture 24